## PHYSICAL CHEMISTRY

Thermodynamics, Structure, and Change

Tenth Edition

Peter Atkins | Julio de Paula

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## FUNDAMENTAL CONSTANTS

| Constant | Symbol | Value |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | Power of 10 | Units |
| Speed of light | c | $2.99792458{ }^{*}$ | $10^{8}$ | $\mathrm{m} \mathrm{s}^{-1}$ |
| Elementary charge | $e$ | 1.602176565 | $10^{-19}$ | C |
| Planck's constant | $h$ | 6.62606957 | $10^{-34}$ | J s |
|  | $\hbar=h / 2 \pi$ | 1.054571726 | $10^{-34}$ | J s |
| Boltzmann's constant | $k$ | 1.3806488 | $10^{-23}$ | J K ${ }^{-1}$ |
| Avogadro's constant | $N_{\text {A }}$ | 6.02214129 | $10^{23}$ | $\mathrm{mol}^{-1}$ |
| Gas constant | $R=N_{\text {A }} k$ | 8.3144621 |  | $\mathrm{J} \mathrm{K}^{-1} \mathrm{~mol}^{-1}$ |
| Faraday's constant | $F=N_{\mathrm{A}} e$ | 9.64853365 | $10^{4}$ | C mol ${ }^{-1}$ |
| Mass |  |  |  |  |
| Electron | $m_{\text {e }}$ | 9.10938291 | $10^{-31}$ | kg |
| Proton | $m_{\mathrm{p}}$ | 1.672621777 | $10^{-27}$ | kg |
| Neutron | $m_{\mathrm{n}}$ | 1.674927351 | $10^{-27}$ | kg |
| Atomic mass constant | $m_{u}$ | 1.660538921 | $10^{-27}$ | kg |
| Vacuum permeability | $\mu_{0}$ | $4 \pi^{*}$ | $10^{-7}$ | $\mathrm{J} \mathrm{s}^{2} \mathrm{C}^{-2} \mathrm{~m}^{-1}$ |
| Vacuum permittivity | $\varepsilon_{0}=1 / \mu_{0} c^{2}$ | 8.854187817 | $10^{-12}$ | $\mathrm{J}^{-1} \mathrm{C}^{2} \mathrm{~m}^{-1}$ |
|  | $4 \pi \varepsilon_{0}$ | 1.112650056 | $10^{-10}$ | $\mathrm{J}^{-1} \mathrm{C}^{2} \mathrm{~m}^{-1}$ |
| Bohr magneton | $\mu_{\mathrm{B}}=e \hbar / 2 m_{\text {e }}$ | 9.27400968 | $10^{-24}$ | $\mathrm{J} \mathrm{T}^{-1}$ |
| Nuclear magneton | $\mu_{\mathrm{N}}=e \hbar / 2 m_{\mathrm{p}}$ | 5.05078353 | $10^{-27}$ | $\mathrm{J} \mathrm{T}^{-1}$ |
| Proton magnetic moment | $\mu_{\mathrm{p}}$ | 1.410606743 | $10^{-26}$ | J T ${ }^{-1}$ |
| $g$-Value of electron | $g_{\text {e }}$ | 2.002319304 |  |  |
| Magnetogyric ratio |  |  |  |  |
| Electron | $\gamma_{\mathrm{e}}=-g_{\mathrm{e}} e / 2 m_{e}$ | -1.001 159652 | $10^{10}$ | C kg ${ }^{-1}$ |
| Proton | $\gamma_{\mathrm{p}}=2 \mu_{\mathrm{p}} / \hbar$ | 2.675222004 | $10^{8}$ | C kg ${ }^{-1}$ |
| Bohr radius | $a_{0}=4 \pi \varepsilon_{0} \hbar^{2} / e^{2} m_{e}$ | 5.291772109 | $10^{-11}$ | m |
| Rydberg constant | $\tilde{R}_{\infty}=m_{\mathrm{e}} e^{4} / 8 h^{3} c \varepsilon_{0}^{2}$ | 1.097373157 | $10^{5}$ | $\mathrm{cm}^{-1}$ |
|  | $h c \tilde{R}_{\infty} / e$ | 13.60569253 |  | eV |
| Fine-structure constant | $\alpha=\mu_{0} e^{2} c / 2 h$ | 7.2973525698 | $10^{-3}$ |  |
|  | $\alpha^{-1}$ | 1.37035999074 | $10^{2}$ |  |
| Second radiation constant | $c_{2}=h c / k$ | 1.4387770 | $10^{-2}$ | m K |
| Stefan-Boltzmann constant | $\sigma=2 \pi^{5} k^{4} / 15 h^{3} c^{2}$ | 5.670373 | $10^{-8}$ | W m ${ }^{-2} \mathrm{~K}^{-4}$ |
| Standard acceleration of free fall | $g$ | $9.80665^{*}$ |  | $\mathrm{m} \mathrm{s}^{-2}$ |
| Gravitational constant | G | 6.67384 | $10^{-11}$ | $\mathrm{Nm}^{2} \mathrm{~kg}^{-2}$ |

* Exact value. For current values of the constants, see the National Institute of Standards and Technology (NIST) website.


# PHYSICAL CHEMISTRY 

## Thermodynamics, Structure, and Change

## Tenth edition

## Peter Atkins

Fellow of Lincoln College, University of Oxford, Oxford, UK

Julio de Paula
Professor of Chemistry, Lewis \& Clark College, Portland, Oregon, USA

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## PREFACE

This new edition is the product of a thorough revision of content and its presentation. Our goal is to make the book even more accessible to students and useful to instructors by enhancing its flexibility. We hope that both categories of user will perceive and enjoy the renewed vitality of the text and the presentation of this demanding but engaging subject.

The text is still divided into three parts, but each chapter is now presented as a series of short and more readily mastered Topics. This new structure allows the instructor to tailor the text within the time constraints of the course as omissions will be easier to make, emphases satisfied more readily, and the trajectory through the subject modified more easily. For instance, it is now easier to approach the material either from a 'quantum first' or a 'thermodynamics first' perspective because it is no longer necessary to take a linear path through chapters. Instead, students and instructors can match the choice of Topics to their learning objectives. We have been very careful not to presuppose or impose a particular sequence, except where it is demanded by common sense.

We open with a Foundations chapter, which reviews basic concepts of chemistry and physics used through the text. Part 1 now carries the title Thermodynamics. New to this edition is coverage of ternary phase diagrams, which are important in applications of physical chemistry to engineering and materials science. Part 2 (Structure) continues to cover quantum theory, atomic and molecular structure, spectroscopy, molecular assemblies, and statistical thermodynamics. Part 3 (Change) has lost a chapter dedicated to catalysis, but not the material. Enzyme-catalysed reactions are now in Chapter 20, and heterogeneous catalysis is now part of a new Chapter 22 focused on surface structure and processes.
As always, we have paid special attention to helping students navigate and master this material. Each chapter opens with a brief summary of its Topics. Then each Topic begins with three questions: 'Why do you need to know this material?,' 'What is the key idea?', and 'What do you need to know already?'. The answers to the third question point to other Topics that we consider appropriate to have studied or at least to refer to as background to the current Topic. The Checklists at the end of each

Topic are useful distillations of the most important concepts and equations that appear in the exposition.
We continue to develop strategies to make mathematics, which is so central to the development of physical chemistry, accessible to students. In addition to associating Mathematical background sections with appropriate chapters, we give more help with the development of equations: we motivate them, justify them, and comment on the steps taken to derive them. We also added a new feature: The chemist's toolkit, which offers quick and immediate help on a concept from mathematics or physics.

This edition has more worked Examples, which require students to organize their thoughts about how to proceed with complex calculations, and more Brief illustrations, which show how to use an equation or deploy a concept in a straightforward way. Both have Self-tests to enable students to assess their grasp of the material. We have structured the end-of-chapter Discussion questions, Exercises, and Problems to match the grouping of the Topics, but have added Topicand Chapter-crossing Integrated activities to show that several Topics are often necessary to solve a single problem. The Resource section has been restructured and augmented by the addition of a list of integrals that are used (and referred to) throughout the text.

We are, of course, alert to the development of electronic resources and have made a special effort in this edition to encourage the use of web-based tools, which are identified in the Using the book section that follows this preface. Important among these tools are Impact sections, which provide examples of how the material in the chapters is applied in such diverse areas as biochemistry, medicine, environmental science, and materials science.
Overall, we have taken this opportunity to refresh the text thoroughly, making it even more flexible, helpful, and up to date. As ever, we hope that you will contact us with your suggestions for its continued improvement.

PWA, Oxford
JdeP, Portland

## USING THE BOOK

For the tenth edition of Physical Chemistry: Thermodynamics, Structure, and Change we have tailored the text even more closely to the needs of students. First, the material within each chapter has been reorganized into discrete topics to improve accessibility, clarity, and flexibility. Second, in addition to
the variety of learning features already present, we have significantly enhanced the mathematics support by adding new Chemist's toolkit boxes, and checklists of key concepts at the end of each topic.

## Organizing the information

## Innovative new structure

Each chapter has been reorganized into short topics, making the text more readable for students and more flexible for instructors. Each topic opens with a comment on why it is important, a statement of the key idea, and a brief summary of the background needed to understand the topic.

> Why do you need to know this material?
> Because chemistry is about matter and the changes that it can undergo, both physically and chemically, the properties of matter underlie the entire discussion in this book.
> What is the key idea?
> The bulk properties of matter are related to the identities

## Notes on good practice

Our Notes on good practice will help you avoid making common mistakes. They encourage conformity to the international language of science by setting out the conventions and procedures adopted by the International Union of Pure and Applied Chemistry (IUPAC).

## Resource section

The comprehensive Resource section at the end of the book contains a table of integrals, data tables, a summary of conventions about units, and character tables. Short extracts of these tables often appear in the topics themselves, principally to give an idea of the typical values of the physical quantities we are introducing.
applicable only to perfect gases (and other idealized systems) are labelled, as here, with a number in blue.

A note on good practice Although the term 'ideal gas' is almost universally used in place of 'perfect gas', there are reasons for preferring the latter term. In an ideal system the interactions between molecules in a mixture are all the same. In a perfect gas not only are the interactions all the same but they are in fact zero. Few, though, make this useful distinction.

Equation A.5, the perfect gas equation, is a summary of three empirical conclusions, namely Boyle's law ( $p \propto 1 / V$ at

## RESOURCE SECTION

## Contents

## 964

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## Checklist of concepts

A Checklist of key concepts is provided at the end of each topic so that you can tick off those concepts which you feel you have mastered.

## Checklist of concepts

1. The entropy acts as a signpost of spontaneous change.
$\square$ 2. Entropy change is defined in terms of heat transactions (the Clausius definition).
$\square$ 3. The Boltzmann formula defines absolute entropies in terms of the number of ways of achieving a configuration.

## Presenting the mathematics

## Justifications

Mathematical development is an intrinsic part of physical chemistry, and to achieve full understanding you need to see how a particular expression is obtained and if any assumptions have been made. The Justifications are set off from the text to let you adjust the level of detail to meet your current needs and make it easier to review material.

## Chemist's toolkits

New to the tenth edition, the Chemist's toolkits are succinct reminders of the mathematical concepts and techniques that you will need in order to understand a particular derivation being described in the main text.

## Mathematical backgrounds

There are six Mathematical background sections dispersed throughout the text. They cover in detail the main mathematical concepts that you need to understand in order to be able to master physical chemistry. Each one is located at the end of the chapter to which it is most relevant.

Justification 3A. 1 Heating accompanying reversible adiabatic expansion

This Justification is based on two features of the cycle. One feature is that the two temperatures $T_{\mathrm{h}}$ and $T_{\mathrm{c}}$ in eqn 3 A .7 lie on the same adiabat in Fig. 3A.7. The second feature is that the energy transferred as heat during the two isothermal stages are

$$
q_{\mathrm{h}}=n R T_{\mathrm{h}} \ln \frac{V_{\mathrm{B}}}{V_{\mathrm{A}}} \quad q_{\mathrm{c}}=n R T_{\mathrm{c}} \ln \frac{V_{\mathrm{D}}}{V_{\mathrm{C}}}
$$

We now show that the two volume ratios are related in a very simple way. From the relation between temperature and volume for reversible adiabatic processes $\left(V T^{k}=\right.$ constant, Topic 2 D$)$ :

## The chemist's toolkit A. 1

Quantities and units
The result of a measurement is a physical quantity that is reported as a numerical multiple of a unit:

$$
\text { physical quantity }=\text { numerical value } \times \text { unit }
$$

It follows that units may be treated like algebraic quantities and may be multiplied, divided, and cancelled. Thus, the expression (physical quantity)/unit is the numerical value (a dimensionless quantity) of the measurement in the specified

## Mathematical background 1 Differentiat

Two of the most important mathematical techniques in the physical sciences are differentiation and integration. They occur throughout the subject, and it is essential to be aware of the procedures involved.

## MB1.1 Differentiation: definitions

Differentiation is concerned with the slopes of functions, such as the rate of change of a variable with time. The formal definition of the derivative, $\mathrm{d} f / \mathrm{d} x$, of a function $f(x)$ is

## Annotated equations and equation labels

We have annotated many equations to help you follow how they are developed. An annotation can take you across the equals sign: it is a reminder of the substitution used, an approximation made, the terms that have been assumed constant, the integral used, and so on. An annotation can also be a reminder of the significance of an individual term in an expression. We sometimes color a collection of numbers or symbols to show how they carry from one line to the next. Many of the equations are labelled to highlight their significance.

$$
w=-n R T \int_{V_{\mathrm{i}}}^{V_{\mathrm{i}}} \frac{\mathrm{~d} V}{V} \stackrel{\text { Integral A. } 2}{=}-n R T \ln \frac{V_{\mathrm{f}}}{V_{\mathrm{i}}}
$$

$$
\begin{array}{ll|l}
\begin{array}{l}
\text { Perfect gas, } \\
\text { reversible, } \\
\text { isothermal }
\end{array} & \begin{array}{l}
\text { Work of } \\
\text { expansion }
\end{array} & \text { (2A.9) }
\end{array}
$$

## Checklists of equations

You don't have to memorize every equation in the text. A checklist at the end of each topic summarizes the most important equations and the conditions under which they apply.

## Checklist of equations

| Property | Equation |
| :--- | :--- |
| Compression factor | $Z=V_{\mathrm{m}} / V_{\mathrm{m}}^{\circ}$ |
| Virial equation of state | $p V_{m}=R T\left(1+B / V_{m}+C / V_{\mathrm{m}}^{3}+\cdots\right)$ |
| van der Waals equation of state | $p=n R T /(V-n b)-a(n / V)^{2}$ |
| Reduced variables | $X_{\mathrm{r}}=X_{\mathrm{m}} / X_{\mathrm{c}}$ |

## Setting up and solving problems

## Brief illustrations

A Brief illustration shows you how to use equations or concepts that have just been introduced in the text. They help you to learn how to use data, manipulate units correctly, and become familiar with the magnitudes of properties. They are all accompanied by a Self-test question which you can use to monitor your progress.

## Brief illustration 1C. 5 <br> Corresponding states

The critical constants of argon and carbon dioxide are given in Table 1C.2. Suppose argon is at 23 atm and 200 K , its reduced pressure and temperature are then

$$
p_{\mathrm{r}}=\frac{23 \mathrm{~atm}}{48.0 \mathrm{~atm}}=0.48 \quad T_{\mathrm{r}}=\frac{200 \mathrm{~K}}{150.7 \mathrm{~K}}=1.33
$$

For carbon dioxide to be in a corresponding state, its pressure and temperature would need to be
$p=0.48 \times(72.9 \mathrm{~atm})=35 \mathrm{~atm} \quad T=1.33 \times 304.2 \mathrm{~K}=405 \mathrm{~K}$
Self-test 1C. 6 What would be the corresponding state of ammonia?

Answer: 53 atm, 539 K

## Worked examples

Worked Examples are more detailed illustrations of the application of the material, which require you to assemble and develop concepts and equations. We provide a suggested method for solving the problem and then implement it to reach the answer. Worked examples are also accompanied by Self-test questions.

Example 3A. 2 Calculating the entropy change for a composite process
Calculate the entropy change when argon at $25^{\circ} \mathrm{C}$ and 1.00 bar in a container of volume $0.500 \mathrm{dm}^{3}$ is allowed to expand to $1.000 \mathrm{dm}^{3}$ and is simultaneously heated to $100^{\circ} \mathrm{C}$.

Method As remarked in the text, use reversible isothermal expansion to the final volume, followed by reversible heating at constant volume to the final temperature. The entropy change in the first step is given by eqn 3A. 16 and that of the second step, provided $C_{V}$ is independent of temperature, by eqn 3A. 20 (with $C_{V}$ in place of $C_{p}$ ). In each case we need to

## TOPIC 3A Entropy

## Discussion questions

3A. 1 The evolution of life requires the organization of a very large number of molecules into biological cells. Does the formation of living organisms violate the Second Law of thermodynamics? State your conclusion clearly and present detailed arguments to support it.
3A. 2 Discuss the significance of the terms 'dispersal' and 'disorder' in the context of the Second Law.

## Exercises

3A.1(a) During a hypothetical process, the entropy of a system increases by $125 \mathrm{~J} \mathrm{~K}^{-1}$ while the entropy of the surroundings decreases by $125 \mathrm{~J} \mathrm{~K}^{-1}$. Is the process spontaneous?
3A.1(b) During a hypothetical process, the entropy of a system increases by $105 \mathrm{~J} \mathrm{~K}^{-1}$ while the entropy of the surroundings decreases by $95 \mathrm{~J} \mathrm{~K}^{-1}$. Is the process spontaneous?
3A.2(a) A certain ideal heat engine uses water at the triple point as the hot source and an organic liquid as the cold sink. It withdraws 10.00 kJ of heat from the hot source and generates 3.00 kJ of work. What is the temperature of the organic liquid?
3A.2(b) A certain ideal heat engine uses water at the triple point as the hot source and an organic liquid as the cold sink. It withdraws 2.71 kJ of heat from the hot source and generates 0.71 kJ of work. What is the temperature of the organic liquid?

The Instructor's Solutions Manual provides full solutions to the 'b' exercises and to the even-numbered problems (available to download from the Book Companion Site for registered adopters of the book only).

## BOOK COMPANION SITE

The Book Companion Site to accompany Physical Chemistry: Thermodynamics, Structure, and Change, tenth edition provides a number of useful teaching and learning resources for students and instructors.

The site can be accessed at:
http://www.whfreeman.com/pchem10e/

Instructor resources are available only to registered adopters of the textbook. To register, simply visit http://www. whfreeman.com/pchem10e/ and follow the appropriate links.

Student resources are openly available to all, without registration.

## @) Materials on the Book Companion Site include:

## 'Impact' sections

'Impact' sections show how physical chemistry is applied in a variety of modern contexts. New for this edition, the Impacts are linked from the text by QR code images. Alternatively, visit the URL displayed next to the QR code image.

## Group theory tables

Comprehensive group theory tables are available to download.

## Figures and tables from the book

Instructors can find the artwork and tables from the book in ready-to-download format. These may be used for lectures without charge (but not for commercial purposes without specific permission).

## Molecular modeling problems

PDFs containing molecular modeling problems can be downloaded, designed for use with the Spartan Student ${ }^{\text {trw }}$ software. However they can also be completed using any modeling software that allows Hartree-Fock, density functional, and MP2 calculations.

## Living graphs

These interactive graphs can be used to explore how a property changes as various parameters are changed. Living graphs are sometimes referred to in the Integrated activities at the end of a chapter.

## ACKNOWLEDGEMENTS

A book as extensive as this could not have been written without significant input from many individuals. We would like to reiterate our thanks to the hundreds of people who contributed to the first nine editions. Many people gave their advice based on the ninth edition, and others, including students, reviewed the draft chapters for the tenth edition as they emerged. We wish to express our gratitude to the following colleagues:

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Because we prepared this edition at the same time as its sister volume, Physical Chemistry: Quanta, matter, and change, it goes without saying that our colleague on that book, Ron Friedman, has had an unconscious but considerable impact on this text too, and we cannot thank him enough for his contribution to this book. Our warm thanks also go to Charles Trapp, Carmen Giunta, and Marshall Cady who once again have produced the Solutions manuals that accompany this book and whose comments led us to make a number of improvements. Kerry Karukstis contributed helpfully to the Impacts that are now on the web.

Last, but by no means least, we would also like to thank our two commissioning editors, Jonathan Crowe of Oxford University Press and Jessica Fiorillo of W. H. Freeman \& Co., and their teams for their encouragement, patience, advice, and assistance.

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## Foundations

Chemistry is the science of matter and the changes it can undergo. Physical chemistry is the branch of chemistry that establishes and develops the principles of the subject in terms of the underlying concepts of physics and the language of mathematics. It provides the basis for developing new spectroscopic techniques and their interpretation, for understanding the structures of molecules and the details of their electron distributions, and for relating the bulk properties of matter to their constituent atoms. Physical chemistry also provides a window on to the world of chemical reactions, and allows us to understand in detail how they take place.

## A Matter

Throughout the text we draw on a number of concepts that should already be familiar from introductory chemistry, such as the 'nuclear model' of the atom, 'Lewis structures' of molecules, and the 'perfect gas equation.' This Topic reviews these and other concepts of chemistry that appear at many stages of the presentation.

## B Energy

Because physical chemistry lies at the interface between physics and chemistry, we also need to review some of the
concepts from elementary physics that we need to draw on in the text. This Topic begins with a brief summary of 'classical mechanics', our starting point for discussion of the motion and energy of particles. Then it reviews concepts of 'thermodynamics' that should already be part of your chemical vocabulary. Finally, we introduce the 'Boltzmann distribution' and the 'equipartition theorem', which help to establish connections between the bulk and molecular properties of matter.

## C Waves

This Topic describes waves, with a focus on 'harmonic waves', which form the basis for the classical description of electromagnetic radiation. The classical ideas of motion, energy, and waves in this Topic and Topic B are expanded with the principles of quantum mechanics (Chapter 7), setting the stage for the treatment of electrons, atoms, and molecules. Quantum mechanics underlies the discussion of chemical structure and chemical change, and is the basis of many techniques of investigation.

## A Matter

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Why do you need to know this material?
Because chemistry is about matter and the changes that it can undergo, both physically and chemically, the properties of matter underlie the entire discussion in this book.

## What is the key idea?

The bulk properties of matter are related to the identities and arrangements of atoms and molecules in a sample.

What do you need to know already?
This Topic reviews material commonly covered in introductory chemistry.

The presentation of physical chemistry in this text is based on the experimentally verified fact that matter consists of atoms.

In this Topic, which is a review of elementary concepts and language widely used in chemistry, we begin to make connections between atomic, molecular, and bulk properties. Most of the material is developed in greater detail later in the text.

## A. 1 Atoms

The atom of an element is characterized by its atomic number, $Z$, which is the number of protons in its nucleus. The number of neutrons in a nucleus is variable to a small extent, and the nucleon number (which is also commonly called the mass number), $A$, is the total number of protons and neutrons in the nucleus. Protons and neutrons are collectively called nucleons. Atoms of the same atomic number but different nucleon number are the isotopes of the element.

## (a) The nuclear model

According to the nuclear model, an atom of atomic number $Z$ consists of a nucleus of charge $+Z e$ surrounded by $Z$ electrons each of charge $-e$ ( $e$ is the fundamental charge: see inside the front cover for its value and the values of the other fundamental constants). These electrons occupy atomic orbitals, which are regions of space where they are most likely to be found, with no more than two electrons in any one orbital. The atomic orbitals are arranged in shells around the nucleus, each shell being characterized by the principal quantum number, $n=1,2, \ldots$. A shell consists of $n^{2}$ individual orbitals, which are grouped together into $n$ subshells; these subshells, and the orbitals they contain, are denoted s, p, d, and f. For all neutral atoms other than hydrogen, the subshells of a given shell have slightly different energies.

## (b) The periodic table

The sequential occupation of the orbitals in successive shells results in periodic similarities in the electronic configurations, the specification of the occupied orbitals, of atoms when they are arranged in order of their atomic number. This periodicity of structure accounts for the formulation of the periodic table (see the inside the back cover). The vertical columns of the periodic table are called groups and (in the modern convention) numbered from 1 to 18 . Successive rows of the periodic table are called periods, the number of the period being equal
to the principal quantum number of the valence shell, the outermost shell of the atom.

Some of the groups also have familiar names: Group 1 consists of the alkali metals, Group 2 (more specifically, calcium, strontium, and barium) of the alkaline earth metals, Group 17 of the halogens, and Group 18 of the noble gases. Broadly speaking, the elements towards the left of the periodic table are metals and those towards the right are non-metals; the two classes of substance meet at a diagonal line running from boron to polonium, which constitute the metalloids, with properties intermediate between those of metals and non-metals.

The periodic table is divided into $\mathrm{s}, \mathrm{p}, \mathrm{d}$, and f blocks, according to the subshell that is last to be occupied in the formulation of the electronic configuration of the atom. The members of the d block (specifically the members of Groups 3-11 in the d block) are also known as the transition metals; those of the f block (which is not divided into numbered groups) are sometimes called the inner transition metals. The upper row of the f block (Period 6) consists of the lanthanoids (still commonly the 'lanthanides') and the lower row (Period 7) consists of the actinoids (still commonly the 'actinides').

## (c) Ions

A monatomic ion is an electrically charged atom. When an atom gains one or more electrons it becomes a negatively charged anion; when it loses one or more electrons it becomes a positively charged cation. The charge number of an ion is called the oxidation number of the element in that state (thus, the oxidation number of magnesium in $\mathrm{Mg}^{2+}$ is +2 and that of oxygen in $\mathrm{O}^{2-}$ is -2 ). It is appropriate, but not always done, to distinguish between the oxidation number and the oxidation state, the latter being the physical state of the atom with a specified oxidation number. Thus, the oxidation number of magnesium is +2 when it is present as $\mathrm{Mg}^{2+}$, and it is present in the oxidation state $\mathrm{Mg}^{2+}$.

The elements form ions that are characteristic of their location in the periodic table: metallic elements typically form cations by losing the electrons of their outermost shell and acquiring the electronic configuration of the preceding noble gas atom. Nonmetals typically form anions by gaining electrons and attaining the electronic configuration of the following noble gas atom.

## A. 2 Molecules

A chemical bond is the link between atoms. Compounds that contain a metallic element typically, but far from universally, form ionic compounds that consist of cations and anions in a crystalline array. The 'chemical bonds' in an ionic compound
are due to the Coulombic interactions between all the ions in the crystal and it is inappropriate to refer to a bond between a specific pair of neighbouring ions. The smallest unit of an ionic compound is called a formula unit. Thus $\mathrm{NaNO}_{3}$, consisting of a $\mathrm{Na}^{+}$cation and a $\mathrm{NO}_{3}^{-}$anion, is the formula unit of sodium nitrate. Compounds that do not contain a metallic element typically form covalent compounds consisting of discrete molecules. In this case, the bonds between the atoms of a molecule are covalent, meaning that they consist of shared pairs of electrons.
A note on good practice Some chemists use the term 'molecule' to denote the smallest unit of a compound with the composition of the bulk material regardless of whether it is an ionic or covalent compound and thus speak of 'a molecule of NaCl '. We use the term 'molecule' to denote a discrete covalently bonded entity (as in $\mathrm{H}_{2} \mathrm{O}$ ); for an ionic compound we use 'formula unit'.

## (a) Lewis structures

The pattern of bonds between neighbouring atoms is displayed by drawing a Lewis structure, in which bonds are shown as lines and lone pairs of electrons, pairs of valence electrons that are not used in bonding, are shown as dots. Lewis structures are constructed by allowing each atom to share electrons until it has acquired an octet of eight electrons (for hydrogen, a duplet of two electrons). A shared pair of electrons is a single bond, two shared pairs constitute a double bond, and three shared pairs constitute a triple bond. Atoms of elements of Period 3 and later can accommodate more than eight electrons in their valence shell and 'expand their octet' to become hypervalent, that is, form more bonds than the octet rule would allow (for example, $\mathrm{SF}_{6}$ ), or form more bonds to a small number of atoms (see Brief illustration A.1). When more than one Lewis structure can be written for a given arrangement of atoms, it is supposed that resonance, a blending of the structures, may occur and distribute multi-ple-bond character over the molecule (for example, the two Kekulé structures of benzene). Examples of these aspects of Lewis structures are shown in Fig. A.1.


Figure A. 1 Examples of Lewis structures.

## Brief illustration A. 1 Octet expansion

Octet expansion is also encountered in species that do not necessarily require it, but which, if it is permitted, may acquire a lower energy. Thus, of the structures (1a) and (1b) of the $\mathrm{SO}_{4}^{2-}$ ion, the second has a lower energy than the first. The actual structure of the ion is a resonance hybrid of both structures (together with analogous structures with double bonds in different locations), but the latter structure makes the dominant contribution.


Self-test A. 1 Draw the Lewis structure for $\mathrm{XeO}_{4}$.

## (b) VSEPR theory

Except in the simplest cases, a Lewis structure does not express the three-dimensional structure of a molecule. The simplest approach to the prediction of molecular shape is valenceshell electron pair repulsion theory (VSEPR theory). In this approach, the regions of high electron density, as represented by bonds-whether single or multiple-and lone pairs, take up orientations around the central atom that maximize their separations. Then the position of the attached atoms (not the lone pairs) is noted and used to classify the shape of the molecule. Thus, four regions of electron density adopt a tetrahedral arrangement; if an atom is at each of these locations (as in $\mathrm{CH}_{4}$ ), then the molecule is tetrahedral; if there is an atom at only three of these locations (as in $\mathrm{NH}_{3}$ ), then the molecule is


Figure A. 2 The shapes of molecules that result from application of VSEPR theory.
trigonal pyramidal, and so on. The names of the various shapes that are commonly found are shown in Fig. A.2. In a refinement of the theory, lone pairs are assumed to repel bonding pairs more strongly than bonding pairs repel each other. The shape a molecule then adopts, if it is not determined fully by symmetry, is such as to minimize repulsions from lone pairs.

## Brief illustration A. 2 Molecular shapes

In $\mathrm{SF}_{4}$ the lone pair adopts an equatorial position and the two axial S-F bonds bend away from it slightly, to give a bent seesaw shaped molecule (Fig. A.3).


Figure A. 3 (a) $\mathrm{In} \mathrm{SF}_{4}$ the lone pair adopts an equatorial position. (b) The two axial S-F bonds bend away from it slightly, to give a bent see-saw shaped molecule.

Self-test A. 2 Predict the shape of the $\mathrm{SO}_{3}^{2-}$ ion.
Answer: Trigonal pyramid

## (c) Polar bonds

Covalent bonds may be polar, or correspond to an unequal sharing of the electron pair, with the result that one atom has a partial positive charge (denoted $\delta+$ ) and the other a partial negative charge ( $\delta-$ ). The ability of an atom to attract electrons to itself when part of a molecule is measured by the electronegativity, $\chi$ (chi), of the element. The juxtaposition of equal and opposite partial charges constitutes an electric dipole. If those charges are $+Q$ and $-Q$ and they are separated by a distance $d$, the magnitude of the electric dipole moment, $\mu$, is
$\mu=Q d \quad$ Definition Magnitude of the electric dipole moment (A.1)

## Brief illustration A. 3 <br> Nonpolar molecules with <br> polar bonds

Whether or not a molecule as a whole is polar depends on the arrangement of its bonds, for in highly symmetrical molecules there may be no net dipole. Thus, although the linear $\mathrm{CO}_{2}$ molecule (which is structurally OCO) has polar CO bonds, their effects cancel and the molecule as a whole is nonpolar.
Self-test A. 3 Is $\mathrm{NH}_{3}$ polar?
Answer: Yes

## A. 3 Bulk matter

Bulk matter consists of large numbers of atoms, molecules, or ions. Its physical state may be solid, liquid, or gas:

A solid is a form of matter that adopts and maintains a shape that is independent of the container it occupies.
A liquid is a form of matter that adopts the shape of the part of the container it occupies (in a gravitational field, the lower part) and is separated from the unoccupied part of the container by a definite surface.
A gas is a form of matter that immediately fills any container it occupies.

A liquid and a solid are examples of a condensed state of matter. A liquid and a gas are examples of a fluid form of matter: they flow in response to forces (such as gravity) that are applied.

## (a) Properties of bulk matter

The state of a bulk sample of matter is defined by specifying the values of various properties. Among them are:

The mass, $m$, a measure of the quantity of matter present (unit: 1 kilogram, 1 kg ).
The volume, $V$, a measure of the quantity of space the sample occupies (unit: 1 cubic metre, $1 \mathrm{~m}^{3}$ ).
The amount of substance, $n$, a measure of the number of specified entities (atoms, molecules, or formula units) present (unit: 1 mole, 1 mol ).

## Brief illustration A. 4 Volume units

Volume is also expressed as submultiples of $1 \mathrm{~m}^{3}$, such as cubic decimetres ( $1 \mathrm{dm}^{3}=10^{-3} \mathrm{~m}^{3}$ ) and cubic centimetres $\left(1 \mathrm{~cm}^{3}=10^{-6} \mathrm{~m}^{3}\right)$. It is also common to encounter the nonSI unit litre ( $1 \mathrm{~L}=1 \mathrm{dm}^{3}$ ) and its submultiple the millilitre ( $1 \mathrm{~mL}=1 \mathrm{~cm}^{3}$ ). To carry out simple unit conversions, simply replace the fraction of the unit (such as 1 cm ) by its definition (in this case, $10^{-2} \mathrm{~m}$ ). Thus, to convert $100 \mathrm{~cm}^{3}$ to cubic decimetres (litres), use $1 \mathrm{~cm}=10^{-1} \mathrm{dm}$, in which case $100 \mathrm{~cm}^{3}=100$ $\left(10^{-1} \mathrm{dm}\right)^{3}$, which is the same as $0.100 \mathrm{dm}^{3}$.

Self-test A. 4 Express a volume of $100 \mathrm{~mm}^{3}$ in units of $\mathrm{cm}^{3}$.
Answer: $0.100 \mathrm{~cm}^{3}$

An extensive property of bulk matter is a property that depends on the amount of substance present in the sample; an intensive property is a property that is independent of the amount of substance. The volume is extensive; the mass density, $\rho$ (rho), with

$$
\begin{equation*}
\rho=\frac{m}{V} \tag{A.2}
\end{equation*}
$$

Mass density
is intensive.
The amount of substance, $n$ (colloquially, 'the number of moles'), is a measure of the number of specified entities present in the sample. 'Amount of substance' is the official name of the quantity; it is commonly simplified to 'chemical amount' or simply 'amount'. The unit 1 mol is currently defined as the number of carbon atoms in exactly 12 g of carbon-12. (In 2011 the decision was taken to replace this definition, but the change has not yet, in 2014, been implemented.) The number of entities per mole is called Avogadro's constant, $N_{A}$; the currently accepted value is $6.022 \times 10^{23} \mathrm{~mol}^{-1}$ (note that $N_{\mathrm{A}}$ is a constant with units, not a pure number).

The molar mass of a substance, $M$ (units: formally kilograms per mole but commonly grams per mole, $\mathrm{g} \mathrm{mol}^{-1}$ ) is the mass per mole of its atoms, its molecules, or its formula units. The amount of substance of specified entities in a sample can readily be calculated from its mass, by noting that

$$
\begin{equation*}
n=\frac{m}{M} \tag{A.3}
\end{equation*}
$$

Amount of substance

A note on good practice Be careful to distinguish atomic or molecular mass (the mass of a single atom or molecule; units kg ) from molar mass (the mass per mole of atoms or molecules; units $\mathrm{kg} \mathrm{mol}^{-1}$ ). Relative molecular masses of atoms and molecules, $M_{\mathrm{r}}=m / m_{\mathrm{u}}$, where $m$ is the mass of the atom or molecule and $m_{\mathrm{u}}$ is the atomic mass constant (see inside front cover), are still widely called 'atomic weights' and 'molecular weights' even though they are dimensionless quantities and not weights (the gravitational force exerted on an object).

A sample of matter may be subjected to a pressure, $p$ (unit: 1 pascal, $\mathrm{Pa} ; 1 \mathrm{~Pa}=1 \mathrm{~kg} \mathrm{~m}^{-1} \mathrm{~s}^{-2}$ ), which is defined as the force, $F$, it is subjected to divided by the area, $A$, to which that force is applied. A sample of gas exerts a pressure on the walls of its container because the molecules of gas are in ceaseless, random motion, and exert a force when they strike the walls. The frequency of the collisions is normally so great that the force, and therefore the pressure, is perceived as being steady.

Although 1 pascal is the SI unit of pressure (The chemist's toolkit A.1), it is also common to express pressure in bar ( $1 \mathrm{bar}=10^{5} \mathrm{~Pa}$ ) or atmospheres ( $1 \mathrm{~atm}=101325 \mathrm{~Pa}$ exactly), both of which correspond to typical atmospheric pressure. Because many physical properties depend on the pressure acting on a sample, it is appropriate to select a certain value of the pressure to report their values. The standard pressure for reporting physical quantities is currently defined as $p^{\ominus}=1$ bar exactly.

## The chemist's toolkit A. 1 <br> Quantities and units

The result of a measurement is a physical quantity that is reported as a numerical multiple of a unit:

$$
\text { physical quantity }=\text { numerical value } \times \text { unit }
$$

It follows that units may be treated like algebraic quantities and may be multiplied, divided, and cancelled. Thus, the expression (physical quantity)/unit is the numerical value (a dimensionless quantity) of the measurement in the specified units. For instance, the mass $m$ of an object could be reported as $m=2.5 \mathrm{~kg}$ or $m / \mathrm{kg}=2.5$. See Table A. 1 in the Resource section for a list of units. Although it is good practice to use only SI units, there will be occasions where accepted practice is so deeply rooted that physical quantities are expressed using other, non-SI units. By international convention, all physical quantities are represented by oblique (sloping) symbols; all units are roman (upright).
Units may be modified by a prefix that denotes a factor of a power of 10 . Among the most common SI prefixes are those listed in Table A. 2 in the Resource section. Examples of the use of these prefixes are:

$$
1 \mathrm{~nm}=10^{-9} \mathrm{~m} \quad 1 \mathrm{ps}=10^{-12} \mathrm{~s} \quad 1 \mu \mathrm{~mol}=10^{-6} \mathrm{~mol}
$$

Powers of units apply to the prefix as well as the unit they modify. For example, $1 \mathrm{~cm}^{3}=1(\mathrm{~cm})^{3}$, and $\left(10^{-2} \mathrm{~m}\right)^{3}=10^{-6} \mathrm{~m}^{3}$. Note that $1 \mathrm{~cm}^{3}$ does not mean $1 \mathrm{c}\left(\mathrm{m}^{3}\right)$. When carrying out numerical calculations, it is usually safest to write out the numerical value of an observable in scientific notation (as $n . n n n \times 10^{n}$ ).
There are seven SI base units, which are listed in Table A. 3 in the Resource section. All other physical quantities may be expressed as combinations of these base units (see Table A. 4 in the Resource section). Molar concentration (more formally, but very rarely, amount of substance concentration) for example, which is an amount of substance divided by the volume it occupies, can be expressed using the derived units of $\mathrm{mol} \mathrm{dm}^{-3}$ as a combination of the base units for amount of substance and length. A number of these derived combinations of units have special names and symbols and we highlight them as they arise.

To specify the state of a sample fully it is also necessary to give its temperature, $T$. The temperature is formally a property that determines in which direction energy will flow as heat when two samples are placed in contact through thermally conducting walls: energy flows from the sample with the higher temperature to the sample with the lower temperature. The symbol $T$ is used to denote the thermodynamic temperature which is an absolute scale with $T=0$ as the lowest point. Temperatures above $T=0$ are then most commonly expressed by using the Kelvin scale, in which the gradations of temperature are expressed as multiples of the unit 1 kelvin ( 1 K ). The Kelvin scale is currently defined by setting the triple point of
water (the temperature at which ice, liquid water, and water vapour are in mutual equilibrium) at exactly 273.16 K (as for certain other units, a decision has been taken to revise this definition, but it has not yet, in 2014, been implemented). The freezing point of water (the melting point of ice) at 1 atm is then found experimentally to lie 0.01 K below the triple point, so the freezing point of water is 273.15 K . The Kelvin scale is unsuitable for everyday measurements of temperature, and it is common to use the Celsius scale, which is defined in terms of the Kelvin scale as

$$
\theta /{ }^{\circ} \mathrm{C}=T / \mathrm{K}-273.15 \quad \text { Definition } \quad \text { Celsius scale } \quad \text { (A.4) }
$$

Thus, the freezing point of water is $0^{\circ} \mathrm{C}$ and its boiling point (at 1 atm ) is found to be $100^{\circ} \mathrm{C}$ (more precisely $99.974^{\circ} \mathrm{C}$ ). Note that in this text $T$ invariably denotes the thermodynamic (absolute) temperature and that temperatures on the Celsius scale are denoted $\theta$ (theta).

A note on good practice Note that we write $T=0$, not $T=0 \mathrm{~K}$. General statements in science should be expressed without reference to a specific set of units. Moreover, because $T$ (unlike $\theta$ ) is absolute, the lowest point is 0 regardless of the scale used to express higher temperatures (such as the Kelvin scale). Similarly, we write $m=0$, not $m=0 \mathrm{~kg}$ and $l=0$, not $l=0 \mathrm{~m}$.

## (b) The perfect gas equation

The properties that define the state of a system are not in general independent of one another. The most important example of a relation between them is provided by the idealized fluid known as a perfect gas (also, commonly, an 'ideal gas'):

$$
\begin{equation*}
p V=n R T \quad \text { Perfect gas equation } \tag{A.5}
\end{equation*}
$$

Here $R$ is the gas constant, a universal constant (in the sense of being independent of the chemical identity of the gas) with the value $8.3145 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$. Throughout this text, equations applicable only to perfect gases (and other idealized systems) are labelled, as here, with a number in blue.

A note on good practice Although the term 'ideal gas' is almost universally used in place of 'perfect gas', there are reasons for preferring the latter term. In an ideal system the interactions between molecules in a mixture are all the same. In a perfect gas not only are the interactions all the same but they are in fact zero. Few, though, make this useful distinction.

Equation A.5, the perfect gas equation, is a summary of three empirical conclusions, namely Boyle's law ( $p \propto 1 / V$ at constant temperature and amount), Charles's law ( $p \propto T$ at constant volume and amount), and Avogadro's principle ( $V \propto n$ at constant temperature and pressure).

## Example A. 1 Using the perfect gas equation

Calculate the pressure in kilopascals exerted by 1.25 g of nitrogen gas in a flask of volume $250 \mathrm{~cm}^{3}$ at $20^{\circ} \mathrm{C}$.

Method To use eqn A.5, we need to know the amount of molecules (in moles) in the sample, which we can obtain from the mass and the molar mass (by using eqn A.3) and to convert the temperature to the Kelvin scale (by using eqn A.4).

Answer The amount of $\mathrm{N}_{2}$ molecules (of molar mass 28.02 $\mathrm{g} \mathrm{mol}^{-1}$ ) present is

$$
n\left(\mathrm{~N}_{2}\right)=\frac{m}{M\left(\mathrm{~N}_{2}\right)}=\frac{1.25 \mathrm{~g}}{28.02 \mathrm{~g} \mathrm{~mol}^{-1}}=\frac{1.25}{28.02} \mathrm{~mol}
$$

The temperature of the sample is

$$
T / \mathrm{K}=20+273.15 \text {, so } T=(20+273.15) \mathrm{K}
$$

Therefore, after rewriting eqn A. 5 as $p=n R T / V$,

$$
\begin{aligned}
p & =\frac{\overbrace{(1.25 / 28.02) \mathrm{mol}}^{n} \times \overbrace{\left(8.3145 \mathrm{JK}^{-1} \mathrm{~mol}^{-1}\right)}^{R} \times \overbrace{(20+273.15) \mathrm{K}}^{\left(2.50 \times 10^{-4}\right) \mathrm{m}^{3}}}{T} \\
& =\frac{(1.25 / 28.02) \times(8.3145) \times(20+273.15)}{2.50 \times 10^{-4}} \frac{\mathrm{~J}}{\mathrm{~m}^{3}} \\
& =\stackrel{\mathrm{Jm}^{-3}=1 \mathrm{~Pa}}{=} 4.35 \times 10^{5} \mathrm{~Pa}=435 \mathrm{kPa}
\end{aligned}
$$

A note on good practice It is best to postpone a numerical calculation to the last possible stage, and carry it out in a single step. This procedure avoids rounding errors. When
we judge it appropriate to show an intermediate result without committing ourselves to a number of significant figures, we write it as n.nnп....

Self-test A. 5 Calculate the pressure exerted by 1.22 g of carbon dioxide confined in a flask of volume $500 \mathrm{dm}^{3}\left(5.00 \times 10^{2} \mathrm{dm}^{3}\right)$ at $37^{\circ} \mathrm{C}$.

Answer: 143 Pa

All gases obey the perfect gas equation ever more closely as the pressure is reduced towards zero. That is, eqn A. 5 is an example of a limiting law, a law that becomes increasingly valid in a particular limit, in this case as the pressure is reduced to zero. In practice, normal atmospheric pressure at sea level (about 1 atm ) is already low enough for most gases to behave almost perfectly, and unless stated otherwise, we assume in this text that the gases we encounter behave perfectly and obey eqn A.5.

A mixture of perfect gases behaves like a single perfect gas. According to Dalton's law, the total pressure of such a mixture is the sum of the pressures to which each gas would give rise if it occupied the container alone:

$$
p=p_{\mathrm{A}}+p_{\mathrm{B}}+\cdots
$$

Dalton's law (A.6)
Each pressure, $p_{\mathrm{J}}$, can be calculated from the perfect gas equation in the form $p_{\mathrm{J}}=n_{\mathrm{J}} R T / V$.

## Checklist of concepts

1. In the nuclear model of an atom negatively charged electrons occupy atomic orbitals which are arranged in shells around a positively charged nucleus.
$\square$ 2. The periodic table highlights similarities in electronic configurations of atoms, which in turn lead to similarities in their physical and chemical properties.3. Covalent compounds consist of discrete molecules in which atoms are linked by covalent bonds.4. Ionic compounds consist of cations and anions in a crystalline array.5. Lewis structures are useful models of the pattern of bonding in molecules.6. The valence-shell electron pair repulsion theory (VSEPR theory) is used to predict the three-
dimensional shapes of molecules from their Lewis structures.
2. The electrons in polar covalent bonds are shared unequally between the bonded nuclei.
3. The physical states of bulk matter are solid, liquid, or gas.
4. The state of a sample of bulk matter is defined by specifying its properties, such as mass, volume, amount, pressure, and temperature.
$\square$ 10. The perfect gas equation is a relation between the pressure, volume, amount, and temperature of an idealized gas.11. A limiting law is a law that becomes increasingly valid in a particular limit.

## Checklist of equations

| Property | Equation | Comment | Equation number |
| :--- | :--- | :--- | :--- |
| Electric dipole moment | $\mu=Q d$ | $\mu$ is the magnitude of the moment | A. 1 |
| Mass density | $\rho=m / V$ | Intensive property | A.2 |
| Amount of substance | $n=m / M$ | Extensive property | A.3 |
| Celsius scale | $\theta /{ }^{\circ} \mathrm{C}=T / \mathrm{K}-273.15$ | Temperature is an intensive property; 273.15 is exact. | A. 4 |
| Perfect gas equation | $p V=n R T$ |  | A. 5 |
| Dalton's law | $p=p_{\mathrm{A}}+p_{\mathrm{B}}+\cdots$ | A. 6 |  |

## B Energy

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## Why do you need to know this material?

Energy is the central unifying concept of physical chemistry, and you need to gain insight into how electrons, atoms, and molecules gain, store, and lose energy.

## What is the key idea?

Energy, the capacity to do work, is restricted to discrete values in electrons, atoms, and molecules.

What do you need to know already?
You need to review the laws of motion and principles of electrostatics normally covered in introductory physics and concepts of thermodynamics normally covered in introductory chemistry.

Much of chemistry is concerned with transfers and transformations of energy, and from the outset it is appropriate to define this familiar quantity precisely. We begin here by reviewing classical mechanics, which was formulated by Isaac Newton in the seventeenth century, and establishes the vocabulary used to describe the motion and energy of particles. These classical ideas prepare us for quantum mechanics, the more fundamental theory formulated in the twentieth century for the study of small particles, such as electrons, atoms, and molecules. We develop the concepts of quantum mechanics throughout the text. Here we begin to see why it is needed as a foundation for understanding atomic and molecular structure.

## B. 1 Force

Molecules are built from atoms and atoms are built from subatomic particles. To understand their structures we need to know how these bodies move under the influence of the forces they experience.

## (a) Momentum

'Translation' is the motion of a particle through space. The velocity, $v$, of a particle is the rate of change of its position $r$ :

$$
\begin{equation*}
v=\frac{\mathrm{d} r}{\mathrm{~d} t} \quad \text { Definition Velocity } \tag{B.1}
\end{equation*}
$$

For motion confined to a single dimension, we would write $v_{x}=\mathrm{d} x / \mathrm{d} t$. The velocity and position are vectors, with both direction and magnitude (vectors and their manipulation are treated in detail in Mathematical background 5). The magnitude of the velocity is the speed, $v$. The linear momentum, $p$, of a particle of mass $m$ is related to its velocity, $v$, by

$$
\begin{equation*}
p=m v \quad \text { Definition } \quad \text { Linear momentum } \tag{B.2}
\end{equation*}
$$

Like the velocity vector, the linear momentum vector points in the direction of travel of the particle (Fig. B.1); its magnitude is denoted $p$.
The description of rotation is very similar to that of translation. The rotational motion of a particle about a central point is described by its angular momentum, $J$. The angular

